

Probing Extended Modes on Disordered Plasmonic Networks by Wavefront Shaping

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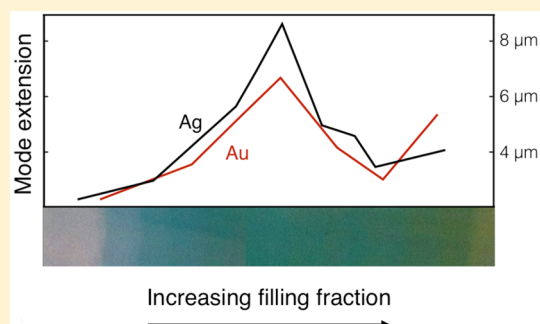
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S Supporting Information

ABSTRACT: We experimentally study the optical field distribution on disordered plasmonic networks by far-field wavefront shaping. We observe nonlocal fluctuations of the field intensity mediated by plasmonic modes up to a distance of 10 μm from the excitation area. In particular we quantify the spatial extent of these fluctuations as a function of the metal filling fraction in the plasmonic network, and we identify a clear increase around percolation due to the existence of extended plasmonic modes. This paves the way toward far-field coherent control of plasmonic modes on similar disordered plasmonic networks. We expect these results to be relevant for quantum networks, coherent control, and light–matter interactions in such disordered films where long-range interactions are critical.

KEYWORDS: plasmonic networks, surface plasmon, surface wave, wavefront shaping, mode extension, disorder, far-field control, leaky wave microscopy



The field of plasmonics offers a unique route for bridging the gap between photonics and the nanometer scale with typical subdiffraction features.^{1,2} In fact, plasmonic structures can efficiently couple propagating light and concentrate it into nanometric volumes, and vice versa.^{1,2} While the location of these hot spots is mostly determined by the geometry of the plasmonic system, their dynamical reconfiguration has potential for applications in sensing,³ photovoltaics,⁴ quantum networks,⁵ nanocircuitry,⁶ metamaterials,⁷ and super-resolution microscopy.⁸ Several strategies borrowed by the field of coherent control have been suggested to reach this goal.^{9–15} But selectivity is limited to a few modes predefined by the sample structure and typically requires advanced fabrication.

Disordered networks, such as dielectrics and metal–dielectric composites, provide a new class of photonic materials to control light propagation and enhance the interaction of light with matter down to the single-molecule level.^{16–18} Disordered semicontinuous metal films, in particular, exhibit intrinsic optical properties that strongly differ from those of bulk metals or ensembles of single nanoparticles, such as broadband absorption^{19–21} and giant field fluctuations.^{22–24} Previous experimental work has tried to quantify the spatial extent of these modes in the near field,^{25–31} where nonradiative components (*dark modes*) dominate over radiative ones (*bright modes*).^{29,32,33} It is not yet clear, therefore, to what extent the plasmonic modes of these systems can be actively controlled from the far field by means of coherent control techniques, thus

allowing for the dynamical reconfigurations of their optical fields at the nanoscale. Other studies have shown^{15,34,35} the existence of long-range interactions on disordered networks.

In this Letter, we experimentally study the optical field distribution on disordered plasmonic networks made of metal–dielectric films by far-field wavefront shaping. Nonlocal fluctuations of the field intensity mediated by plasmonic modes are observed. The spatial extent of these fluctuations is quantified with the introduction of an *interaction length*. This interaction length depends on the metal filling fraction and, in particular, shows a clear increase around percolation that we relate to the existence of extended plasmonic modes. Correlation of these intensity fluctuations indicates that long-range interactions are mediated by a few modes only.

EXPERIMENTAL METHODS

In order to study these metal–dielectric films by means of wavefront shaping, an inverted microscope in leaky wave configuration³⁶ is combined with a phase-only spatial light modulator (SLM) (Figure 1a). A diode pumped solid-state laser source at 785 nm (DPSSL, Oxxius) illuminates the SLM (Boulder Non Linear, 256 \times 256 pixels), which allows up to a 2π phase-shift. Three lenses and an oil-immersion objective

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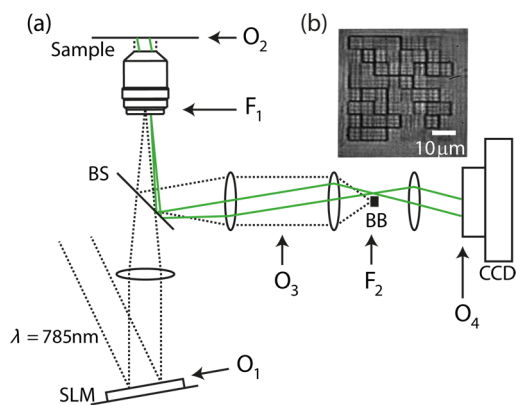


Figure 1. (a) Experimental setup: light from a laser source (not shown) illuminates with a small incident angle ($<5^\circ$) a phase-only SLM (spatial light modulator). The latter is imaged on the sample surface with an oil-immersion objective (NA = 1.4, 60 \times). The same objective images the film surface on a CCD camera via a beam splitter (BS). A beam block (BB) is installed in the Fourier plane of the sample surface along the detection path to remove ballistic light. O_1 , O_2 , O_3 , and O_4 are the position of the object optical plane (i.e., sample plane); F_1 and F_2 are the position of the Fourier optical plane (back focal plane of the microscope objective) along the light path. (b) Image of a typical pattern of the SLM on the sample surface.

(NA = 1.4, 60 \times) image the SLM surface onto the sample plane with a 136 \times reduction. In this configuration, the illumination beam covers a 50 μm radius area, and one macropixel (the binning used in this experiment corresponds to 2×2 pixels of the SLM) covers $350 \times 350 \text{ nm}^2$ on the sample surface, a surface slightly bigger than the one given by the diffraction-limited spot size (280 nm in the present configuration).

The sample is illuminated by the pattern imposed by the SLM and imaged on a CCD camera. A beam block in an intermediate Fourier plane along the detection path allows us to filter direct reflection from the sample.³⁶ The samples under study are disordered metal–dielectric films; they are naturally generated by electron-beam deposition of a thin layer of noble metals, such as gold or silver, on a glass substrate in a vacuum chamber. For a given deposition, the filling fraction is defined as $ff = s_m / (s_m + s_g)$, where s_m and s_g are the surfaces covered by the metal and the glass, respectively; it can be controlled by varying the amount of deposited material and characterized by AFM imaging. Figure 2a and b show increasing thickness from pure glass to an almost continuous metal film respectively for silver and gold. The change of color with the thickness is connected to a change in the filling fraction and the presence of a percolation threshold in the film that induces different plasmonic resonances. The increase of filling fraction with the mass equivalent thickness of the metal, i.e., the average thickness calculated from the deposited metal mass per surface unit, is shown in Figure 2c for both gold and silver.

RESULTS AND DISCUSSION

In disordered metal films, plasmonic modes can be easily coupled to the far field under any incidence. While previous works focused on the subwavelength features of these plasmonic modes, i.e., mainly their hot spots, there is no study that clearly quantifies the existence of bright extended modes with respect to the filling fraction on a scale larger than the wavelength. Yet, quantifying this information about these bright modes would be crucial for far-field control.

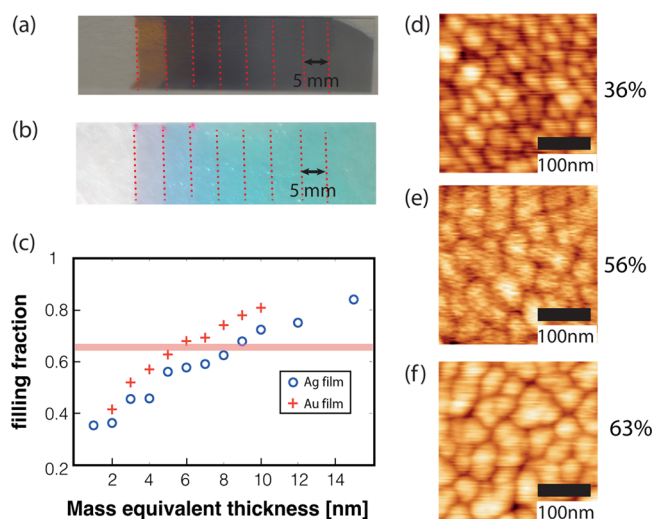


Figure 2. Photos of (a) silver and (b) gold films with increasing thickness from left (no metal) to right (almost continuous film). The vertical dashed lines delimit each incremental step in film thickness. The color change with film thickness is a characteristic of the specific light interaction with semicontinuous noble metal films around the percolation threshold. (c) Filling fraction with the mass equivalent thickness of metal, for gold and silver on a glass substrate, measured from high-resolution atomic force microscopy images. The horizontal bar shows the position where the percolation threshold occurs. (d–f) $300 \times 300 \text{ nm}^2$ high-resolution atomic force microscopy images for silver films with filling fractions (ff) of 0.36 (d), 0.56 (e), and 0.63 (around percolation) (f).

Disordered metal films are known to suffer from very strong scattering. The scattering that is not blocked by the beam block might prevent the detection of local variations, like those from plasmon scattering. Therefore, in order to get statistically relevant measurements of extended modes, we developed the following protocol: the film is illuminated with an SLM pattern uniform in amplitude but with a phase that can be spatially and temporally modulated. The phase pattern is chosen to be spatially random, with a local phase uniformly distributed between 0 and 2π . The spatial phase distribution over the lower part of the SLM pattern is kept constant, while the upper part of the SLM pattern is allowed to randomly evolve (Figure 3a).

If the excitation of the optical fields on the films is only local, there should be no variation of the measured intensity in the area of the image corresponding to the lower part of the SLM pattern. Alternatively, any temporal fluctuation in this area should arise from nonlocal excitation coming from the upper part of the SLM pattern. In order to highlight fluctuations, we calculated the variance of the intensity images $I(x, y, t)$, which is proportional to the variance of the modulated component of the electric field, $E_{\text{mod}}(x, y, t)$ (see Supporting Information):

$$\sigma^2(E_{\text{mod}}(x, y, t)) \propto \frac{\sigma^2(I(x, y, t))}{I(x, y)} \quad (1)$$

where $I(x, y) = \overline{I(x, y, t)}$ is the temporal average of the intensity. In fact, the local amplitude is the coherent sum of a stationary component due to the constant excitation from the lower part of the SLM pattern and a modulated component that we want to quantify coming from the upper part of the SLM pattern. In order to collect sufficient statistics for each filling fraction, we acquire a sequence of 100 images with a two-second integration time corresponding to different excitation phase patterns

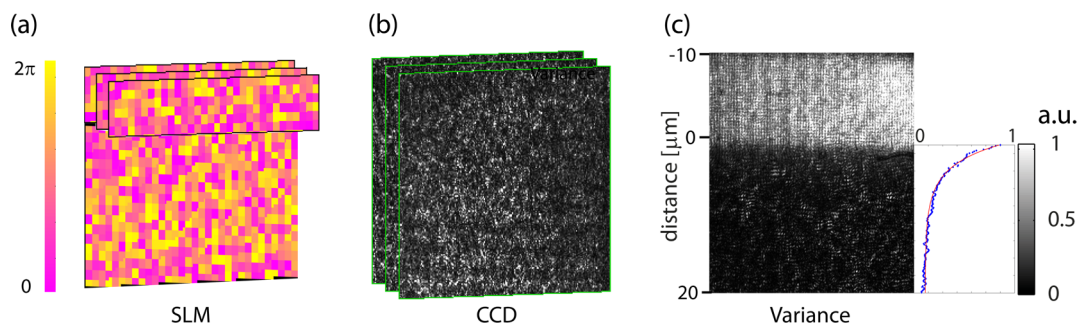


Figure 3. (a) Sequence of random SLM patterns, where only the top horizontal pattern varies. (b) CCD images of the sample under the random illumination patterns of the SLM shown in (a). (c) Normalized variance of 100 different CCD images. The upper band, i.e., the launching zone, corresponds to the part of the sample where the random incident illumination varies. On the far right: spatial average of the variance along the horizontal direction showing how the launching zone influences the lower part of the images. The red line is an exponential fit, from which the interaction length is extracted.

(Figure 3b). Every image is normalized by the incident laser power.

The decay of the variance is computed as a function of the distance x from the modulated part by averaging the variance image horizontally (Figure 3c). This decay is represented by the dotted line, while the continuous line shows a fitting to an exponential function $e^{-x/L}$. In order to extract a relevant parameter to quantify the spatial extent of nonlocal excitations, we define the interaction length as the decay length L of this exponential fitting. To evaluate the resolution limit of this measurement, we measured this decay length L on a continuous layer of copper thicker than 30 nm, a nonplasmonic metal in the visible range, where no propagation is expected at all, and obtained $L_{\text{Cu}} = 1.6 \mu\text{m}$. We attribute this limit of resolution to scattering and spurious reflections of the optical setup. Above this limit, the values of L correspond to long-range interactions in the film. In the following, we study how L varies as a function of the silver filling fraction, ff (Figure 4a),

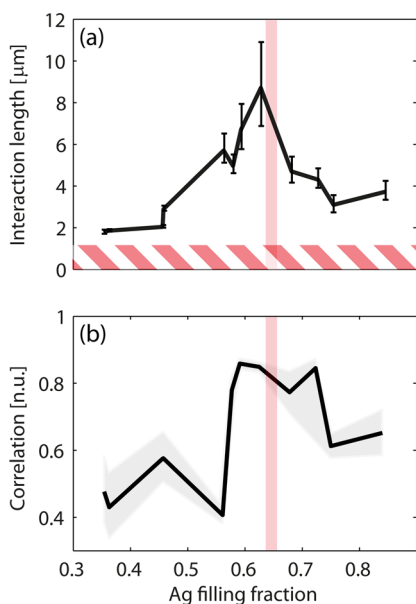


Figure 4. (a) Interaction length (L) for different silver filling fractions (ff). The horizontal dashed stripe shows the detection limit as measured on a continuous layer of copper. (b) Correlation of the intensity C_L for different silver filling fractions (ff). Error bars show measurement variance at different areas of the sample, and the vertical line is the position of the percolation threshold.

well below percolation ($ff < 0.5$), around percolation ($0.5 < ff < 0.7$), and above percolation ($ff > 0.7$).²⁹ Error is evaluated by calculation of the variance at different areas of the sample. We also introduce a second parameter, which plays an important role for nonlocal coupling, i.e., the number of modes contributing to the intensity fluctuations. At a given distance from the temporally modulated area, the image of the intensity correlation at the same point is calculated for different times. It gives information about the number of plasmonic modes that locally contribute to intensity variations. Close to the modulated region, we expect the correlation to be close to zero, as many modes of different spatial extent contribute, while the correlation should reach values close to one very far away from the modulated zone because of the lack of fluctuations. In particular, we decided to calculate the correlation C_L at L in order to quantify how many modes contribute to the interaction length L (Figures.4b).

Below percolation ($ff < 0.5$) particles are far apart and modes are expected to be localized around metal aggregates. The measured interaction length is indeed around $2 \mu\text{m}$, on the order of the maximum particle size, and the correlation C_L is around 0.5, indicating that several modes contribute at a shorter distance L . At high filling fractions ($ff > 0.7$), when the metal layer is almost continuous and one could expect the presence of propagating surface plasmons (SPPs), the interaction length is longer and the correlation C_L is on the order of 0.7, showing that fewer long-range modes are present: the values of L are however lower than what is usually found with continuous silver films given that, for the filling fractions used in this experiment, the metal film is still not continuous and its thickness is far from the optimum value for SPP propagation.³⁷ The interesting regime is around percolation ($0.5 \leq ff \leq 0.7$),²⁹ where hot spots have been observed in the near field²⁵ and extended modes theoretically predicted.³⁸ Compared to the two other regimes, the interaction length L shows a clear increase, reaching an average of up to $8 \mu\text{m}$ at $ff = 0.63$, where the correlation C_L approaches 0.9. We interpret this result as the existence of only one dominant excited electromagnetic mode. Our correlation analysis is thus coherent with the decrease of the resonantly excited modes observed by Seal et al.,²⁶ although not equivalent to previous studies on disordered plasmonic film.^{27,29,39} The latter are dealing with the near-field regime where dark modes with very small extension³² are predominant, giving rise to the regime around percolation where modes are mostly localized.³³ Here we probe bright modes whose extension has never been extensively studied

experimentally on such random networks. The observed interaction length of $8\ \mu\text{m}$ is surprisingly long for silver at this wavelength. Yet Jess M. Gunn et al. found much longer interactions with two-photon luminescence on similar, although not identical, objects.³⁴

To verify the reproducibility and generality of this behavior, we measured the interaction length on gold, a widely used plasmonic material, and compared these measurements with the previous ones on silver (Figure 5). We observe a similar

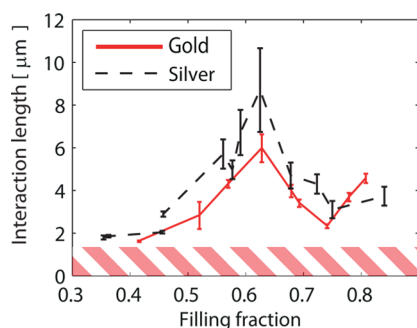


Figure 5. Comparison of the interaction length (L) measured on gold and silver films for different filling fractions (ff). Percolation is around $ff = 0.65$. The shaded stripe shows the detection limit of our detection system as measured on a continuous layer of copper.

increase of the interaction length around percolation also for gold, although L is lower in gold than in silver because of higher absorption at the experimental wavelength ($\text{Re}[\epsilon_{\text{Au}}] = -24$ and $\text{Re}[\epsilon_{\text{Ag}}] = -31$ ⁴⁰).

CONCLUSION

We presented a method to characterize the nonlocal fluctuations of the field intensity on random plasmonic networks. This methodology can be readily adapted to other 2D and 3D random networks. In particular, the measured fluctuations on random plasmonic networks are associated with the existence of bright modes excited and detected from the far field. They correspond to a subpopulation of the total number of modes existing on these films.³⁸ An important result of our analysis is the existence of long-range interactions around percolation that extend up to several micrometers. Correlation studies of these fluctuations point out a reduction of the number of bright modes around percolation. This is linked to the peculiar interaction of light with such films and could be analogous to the existence of a single extended mode on 2D random networks.^{24,41} The possibility of interacting with these extended modes from the far-field has important applications for quantum networks, coherent control, and light–matter interactions at the nanoscale.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsp Photonics.5b00394.

Additional details (PDF)

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Notes

The authors declare no competing financial interest.

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